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**ELECTRONIC IMAGING SYSTEM HAVING A SENSOR FOR  
CORRECTING PERSPECTIVE PROJECTION DISTORTION**

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# **ELECTRONIC IMAGING SYSTEM HAVING A SENSOR FOR CORRECTING PERSPECTIVE PROJECTION DISTORTION**

## **FIELD OF THE INVENTION**

5                   The present invention relates generally to imaging systems and, in particular, to an imaging system for capturing non-planar projections of a scene.

## **BACKGROUND OF THE INVENTION**

10                   Conventional cameras provide photographs of real world scenes with a limited field of view of the scene being photographed. In many scenarios, the photographer desires an image corresponding to a wider field of view. Typically, the photographer can resort to two methods of generating a wide field of view image. The first method is to  
15                   capture the wide field of view image directly; e.g., with a wide-angle lens, or with a specialized system of mirrors to reflect the wide field of view onto the sensor. The second method is to capture a collection of images, each image having a narrower field of view, and then use one of a variety of digital image stitching techniques to combine the narrow field of view  
20                   images into a composite digital image. The composite digital image will appear to be a single wide field of view image.

                  When a camera captures an image of a scene, the image represents a perspective projection of the scene onto the planar sensor. Inherent to perspective projection is a natural distortion, namely, objects  
25                   closer to the center of the image appear smaller than similar objects near the edges of the image. This distortion becomes immediately apparent when attempting to stitch subsequent images together. Therefore, typical image stitching systems include a step of warping the images to compensate for this perspective distortion. In a physical sense, the  
30                   perspective distortion would not exist if the sensor were not planar, but rather spherical (with the radius of the sphere depending on the focal

length of the lens). In scenarios where the sequence of images to be stitched is captured by rotating a camera on a tripod (or rotating a camera about a vertical axis), the perspective distortion would not exist in the horizontal direction if the sensor were cylindrical (with the radius of the cylinder depending on the focal length of the lens, and the axis of the cylinder lying on the axis of rotation of the camera). Even though there would still be distortion in the vertical direction of the images, this distortion would not hamper the photographer's ability to seamlessly stitch together such a sequence of images.

Since it is extremely difficult and expensive to manufacture sensors that are spherical or cylindrical in shape, compensation for the perspective distortion is generally performed after the image has been captured. The compensation is performed by geometrically warping the image so that it appears to have been captured on the spherical or cylindrical sensor. In the article “Panoramic Stereo Imaging System with Automatic Disparity Warping and Seaming” by H.-C. Huang and Y.-P. Hung (Graphical Models and Image Processing, Vol. 60, No. 3, May, 1998, pp. 196-208), the authors derive the equations relating pixels of a cylindrical sensor to that of a planar sensor. The derivation of the equations relating pixels of a spherical sensor to that of a planar sensor is similar. For the spherical sensor, the pixel  $(x, y)$  of the compensated image  $\tilde{\mathbf{I}}$  is related to the captured image  $\mathbf{I}$  by the relationship:

$$\tilde{\mathbf{I}}(x, y) = \mathbf{I}\left(f \tan\left(x p_x f^{-1}\right) / p_x, f \tan\left(y p_y f^{-1}\right) / p_y\right),$$

where  $p_x$  and  $p_y$  are the horizontal and vertical pixel sizes, respectively,  $f$  is the focal length, and  $(x, y) = (0, 0)$  corresponds to the center of the image. For the cylindrical sensor, the pixel  $(x, y)$  of the compensated image  $\tilde{\mathbf{I}}$  is related to the captured image  $\mathbf{I}$  by the relationship:

$$\tilde{\mathbf{I}}(x, y) = \mathbf{I}\left(f \tan\left(x p_x f^{-1}\right) / p_x, y f \tan\left(x p_x f^{-1}\right) / x p_x\right), \text{ for } x \neq 0, \text{ and} \\ \tilde{\mathbf{I}}(0, y) = \mathbf{I}(0, y).$$

After each image in the sequence has been geometrically warped, typical image stitching systems then determine the parameters that optimally align the set of images (for example, by cross correlation or phase correlation, or by knowledge of the geometry of the camera at each capture position). Once the images are aligned, they are blended together (by taking weighted averages of overlapping pixels, for example) to form a composite digital image. Finally, depending on the choice of output, the composite digital image can be again geometrically warped, this time to simulate a perspective projection of the wide field of view scene onto a chosen reference planar sensor.

In some image stitching systems, specifically systems that construct composite digital images in real time, or systems that construct a large sequence of composite digital images (e.g., a system that stitches together images from video sequences to form a composite video sequence), the step of geometrically warping the images to compensate for the perspective distortion requires a significantly large portion of the total computational time of the system. Therefore, any mechanism that would alleviate the need to perform geometric warping of the images would remove this bottleneck in real-time or video image stitching systems.

Another type of distortion that occurs in most camera systems (especially those with wide-angle lenses) is lens distortion. Lens distortion frequently manifests itself as a radial distortion, where objects further from the center of the image appear smaller than those near the center of the image. In addition, lens irregularities and aberrations can induce local distortions in different areas of the image plane.

A method exists in the art to compensate for lens distortion without geometrically warping the images after they have been captured. U.S. Patent No. 5,489,940, "Electronic Imaging System and Sensor for Correcting the Distortion in a Wide-Angle Lens", and U.S. Patent No. 5,739,852, "Electronic Imaging System and Sensor for Use Therefor with

a Nonlinear Distribution of Imaging Elements”, both by C. Richardson and B. Stuckman, describe an imaging system comprising a sensor with a nonlinear distribution of sensor elements, wherein the distribution of the imaging elements corrects for the distortion in a wide angle lens. More specifically, the distribution of sensor elements has a relatively low density at a center point of the sensor surface and a relatively high density along the periphery of the sensor surface. However, neither of these patents are directly applicable to systems compensating for perspective distortion. Perspective distortion, as discussed previously, can be compensated for by projecting the image onto a nonplanar surface. Lens distortion, in the method of the two aforementioned patents, is compensated by projecting the image through a nonlinear function. This nonlinear function is selected such that the scene appears to be projected onto a planar surface, as expected by perspective projection. However, the relative densities of the distribution of sensor elements near the center and periphery of the image are inversely related to what the relative densities should be to compensate for perspective distortion. Consequently, when using digital stitching techniques to combine multiple images captured from the type of sensor disclosed in these patents, a geometric warping must still be applied to overcome the perspective projection.

Therefore, there exists a need in the art for an imaging system that would alleviate the need to perform geometric warping of images to compensate for perspective distortion after the images have been captured.

## SUMMARY OF THE INVENTION

The present invention is directed to overcoming one or more of the problems set forth above. Briefly summarized, according to one aspect of the present invention, an electronic imaging system for capturing an image of a scene includes an optical system for producing an optical image of the scene, an

imaging sensor having a surface in optical communication with the optical system, and a plurality of imaging elements distributed on the surface of the imaging sensor according to a distribution representable by a nonlinear function in which the relative density of the distributed imaging elements is greater toward  
5 the center of the sensor. Such a distribution provides physical coordinates for the imaging elements corresponding to a projection of the scene onto a non-planar surface, thereby compensating for perspective distortion of the scene onto the non-planar surface and alleviating the need to perform geometric warping of the images after they have been captured.

10 These and other aspects, objects, features and advantages of the present invention will be more clearly understood and appreciated from a review of the following detailed description of the preferred embodiments and appended claims, and by reference to the accompanying drawings.

#### 15 **BRIEF DESCRIPTION OF THE DRAWINGS**

Fig. 1 shows a pictorial diagram of a camera used in conjunction with one embodiment of the present invention.

Fig. 2 presents a schematic representation of one embodiment of the present invention.

20 Fig. 3 shows a top view of an integrated circuit implementation of a sensor in accordance with one embodiment of the present invention.

Fig. 4 shows a top view of an integrated circuit implementation of a sensor in accordance with an alternative embodiment  
25 of the present invention.

Fig. 5 presents a tabular diagram of the image data produced, by address of the corresponding imaging element, in accordance with one embodiment of the present invention.

Fig. 6 is a top view of an imaging sensor in accordance  
30 with an embodiment of the present invention.

Fig. 7 is a top view of an imaging sensor in accordance with an alternative embodiment of the present invention.

Fig. 8 shows a pictorial diagram of the geometric relationship between the image sensor and the nonplanar surface in accordance with one embodiment of the present invention.

Fig. 9 shows a pictorial diagram of the geometric relationship between the image sensor and the nonplanar surface in accordance with an alternative embodiment of the present invention.

Fig. 10 presents a block diagram of an electronic imaging system in accordance with a further embodiment of the present invention.

Fig. 11 presents a block diagram of an electronic imaging system in accordance with an alternative further embodiment of the present invention.

## **DETAILED DESCRIPTION OF THE INVENTION**

Because imaging systems employing electronic sensors are well known, the present description will be directed in particular to elements forming part of, or cooperating more directly with, apparatus in accordance with the present invention. Elements not specifically shown or described herein may be selected from those known in the art. Certain aspects of the embodiments to be described may be provided in software. Given the system as shown and described according to the invention in the following materials, software not specifically shown, described or suggested herein that is useful for implementation of the invention is conventional and within the ordinary skill in such arts.

Figure 1 shows a pictorial diagram of a camera used in conjunction with one embodiment of the present invention. Camera **100** includes an optical system, including a lens **102**, that projects an image of the scene in front of camera **100** onto an imaging sensor **104**. This sensor **104** includes an array of individual imaging elements which are

nonlinearly distributed in such a fashion as to automatically correct for the distortion induced by a perspective projection.

Figure 2 presents a schematic representation of one embodiment of the present invention. The sensor **104** is provided for use in an electronic imaging system in which the lens **102** produces an optical image **200**. This image is distorted by the perspective projection. The sensor includes a surface **202** in optical communication with the lens **102**. The sensor further includes a plurality of imaging elements, such as imaging element **204**, coupled to the surface for converting the optical image into a corresponding output signal on an output line **206**. The plurality of imaging elements **204** has a distribution on the surface representable by a nonlinear function, wherein the distribution of the imaging elements simulates the projection of the image onto a nonplanar surface and thus corrects the perspective distortion in the image. Therefore, the output signal **206** corresponds to a perspective distortion corrected image.

Figure 3 shows a top view of an integrated circuit implementation of the sensor **104** in accordance with one embodiment of the present invention. Chip body **300** includes a circular array **302** of imaging elements of which example elements **304**, **306**, and **308** are shown. One must appreciate that the circular array **302** can include thousands, even millions or more, of the imaging elements such as **304**, **306** and **308**, which, in a preferred embodiment are pixels of a charge-coupled device (CCD) or CMOS imager of the kind used in many applications as imaging sensors, particularly in electronic imaging systems. Note that the imaging elements may all have similar sensitivities to light, or the imaging elements may be sensitized to different portions of the visible spectrum, using color filter arrays such as described in U.S. Patent 3,971,065. Axis **310** includes rectangular coordinate vectors  $x$  and  $y$  about an origin in the center of circular array **302**.



In prior art sensors, these imaging elements are distributed uniformly about the surface of the integrated circuit on which they reside. Examples of prior art systems are described in U.S. Pat. No. 4,602,289, issued to Sekine, and in "a Device Structure and Spatial Spectrum for Checker-Pattern CCD Color Camera," IEEE Journal of Solid-State Circuits, Vol. SC13, No. 1, February 1978. In other prior art sensors, the distribution is nonlinear. Examples of such prior art systems are described in the aforementioned U.S. Patent Nos. 5,489,940 and 5,739,852, issued to Richardson and Stuckman, and in U.S. Patent No. 6,201,574, issued to Martin, which are incorporated herein by reference. (Like the other patents, Martin corrects for a wide angle field of view, in this case from a fisheye lens.) In the systems described in these patents, the nonlinear distribution of imaging elements corrects for lens distortion of a wide-angle lens. In particular, as described in the aforementioned U.S. Patent Nos. 5,739,940, 5,489,940 and 6,201,574, the nonlinear distribution of imaging elements has a relatively low density at a center point of the surface and a relatively high density at a point along the periphery of the surface. The current invention differs from all of these systems in that the nonlinear distribution of imaging elements simulates the projection of the image onto a nonplanar surface and thus corrects for perspective distortion (and not only in systems with wide-angle lenses). Furthermore, this nonlinear distribution departs from the prior art in that it has a relatively high density at a center point of the surface and a relatively low density at a point along the periphery of the surface.

Figure 4 shows a top view of an integrated circuit implementation of the sensor **104** in accordance with an alternative embodiment of the present invention. In this embodiment, the sensor **104** has a rectangular array **400** that generates a rectangular portion (**400**) of the image **402** produced by the lens **102**. Each of the sensing elements **304**, **306** and **308** has a unique two-dimensional address that allows the

particular sensing element to be electronically accessed. The address of an arbitrary sensing element can be represented by the coordinate pair  $(a,b)$ . The physical location on the sensor **104** of a sensing element **204** having an address  $(a,b)$  is given by  $(x,y)$  as follows:

5 
$$x = R \cos \left( (Ta/180) (n^2 + m^2)^{-1/2} \right), \text{ and}$$
$$y = R \sin \left( (Tb/180) (n^2 + m^2)^{-1/2} \right),$$

where  $(n,m)$ ,  $(-n,m)$ ,  $(n,-m)$  and  $(-n,-m)$  are rectangular coordinates of the physical boundaries of the rectangular sensing array **400**,  $R$  is the maximum radius of the two-dimensional array (where the origin is the center of the image **402**), and  $T$  is the maximum angle captured by the lens (in degrees).

While the embodiments of the present invention present an addressing system whose origin is the center of the image, one of ordinary skill in the art will recognize that an arbitrary offset can be added to the address components in any dimension without loss of generality.

Figure 5 presents a tabular diagram of the image data produced by address  $(a,b)$  of the corresponding imaging element, in accordance with one embodiment of the present invention. The addresses **502** of the image data **500**, derived from the output signal produced by the sensor in this embodiment, are shown with the origin **504** corresponding to the address  $(0,0)$ . Each of the addresses corresponds to a single pixel of the image to be displayed, wherein the pixel address is the address of the imaging element. Due to the nonlinear distribution of sensing elements and the linear addressing, the sensing element described above provides output image data which is corrected for the distortion introduced by the perspective projection of the image onto the sensor without the need of complex mathematical transform circuitry.

Figure 6 is a top view of an imaging sensor in accordance with an embodiment of the present invention. Imaging sensor **600**

includes an array of imaging elements **602** that is nonlinearly distributed. In particular, the nonlinear distribution of four-hundred and forty-one pixels in array **602** corresponds to an example of the sensor of the present invention where the physical coordinates of each imaging element  
5 correspond to the projection of the scene onto a cylindrical surface. The physical location of each sensor element can be described by the aforementioned formula:

$$\tilde{\mathbf{I}}(x, y) = \mathbf{I}\left(f \tan\left(x p_x f^{-1}\right) / p_x, y f \tan\left(x p_x f^{-1}\right) / x p_x\right), \text{ for } x \neq 0, \text{ and} \\ \tilde{\mathbf{I}}(0, y) = \mathbf{I}(0, y),$$

10 where pixel  $(x, y)$  of the cylindrical image  $\tilde{\mathbf{I}}$  is related to a planar image  $\mathbf{I}$  containing four-hundred and forty-one pixels in a uniform rectilinear array.

Figure 7 is a top view of an imaging sensor in accordance with an alternative embodiment of the present invention. Imaging sensor  
15 **700** includes an array of imaging elements **702** that is nonlinearly distributed. In particular, the nonlinear distribution of four-hundred and forty-one pixels in array **702** corresponds to an example of the sensor of the present invention where the physical coordinates of each imaging element correspond to the projection of the scene onto a spherical surface.  
20 The physical location of each sensor element can be described by the aforementioned formula:

$$\tilde{\mathbf{I}}(x, y) = \mathbf{I}\left(f \tan\left(x p_x f^{-1}\right) / p_x, f \tan\left(y p_y f^{-1}\right) / p_y\right),$$

where pixel  $(x, y)$  of the spherical image  $\tilde{\mathbf{I}}$  is related to a planar image  $\mathbf{I}$  containing four-hundred and forty-one pixels in a uniform rectilinear  
25 array. As shown in both Figures 6 and 7, the imaging elements (**602**, **702**) are distributed on the surface of the imaging sensor (**600**, **700**) according to a distribution representable by a non-linear function in which the relative density of the distribution is greater toward the center of the sensor.

Figure 8 depicts a geometric representation of an imaging sensor **800**, and corresponding cylindrical surface **802** onto which the image projection is simulated. In this embodiment, the nodal point **804** of the lens intersects the cylindrical axis **806**. The radius  $r(f)$  of the cylinder is dependent on the focal length  $f$ . Preferably,  $r(f) = f$ .

Figure 9 depicts a geometric representation of an imaging sensor **900**, and corresponding spherical surface **902** onto which the image projection is simulated. In this embodiment, the nodal point **904** of the lens is located at the center of the sphere. The radius  $r(f)$  of the sphere is dependent on the focal length  $f$ . Preferably,  $r(f) = f$ .

Figure 10 presents a block diagram of an electronic imaging system in accordance with a further embodiment of the present invention. The system includes a lens **1000** for producing an optical image **1002**, and an image sensor **1004** having a surface in optical communication with the lens. This sensor **1004** converts the optical image **1002** into a corresponding output signal **1006**. The imaging sensor **1004** includes a plurality of imaging elements, the plurality of imaging elements having a distribution on the surface representable by a nonlinear function, wherein the distribution of the imaging elements corrects for the distortion in the image **1002** induced by the projection of the optical image onto the planar sensor. Therefore, the output signal **1006** is free of perspective distortion. As shown in broken line, the preceding components may be included in a digital camera **1007**.

At least two output signals are generated to form source digital images **1008**. The source digital images are combined in an image combining step **1010** to form a composite digital image **1012**. The image combining step **1010** typically includes an alignment step, where the source digital images **1008** are aligned either by estimating the alignment parameters with the image data (for example, by cross correlation or phase correlation), or by knowledge of the relative geometry of the camera

system between subsequent captures. The image combining step **1010** also typically includes an image blending step, where the source digital images **1008** are blended together (for example, by taking weighted averages of pixel values in the overlap regions). Such a system for  
5 combining images is described in the aforementioned reference, H.-C. Huang and Y.-P. Hung, "Panoramic Stereo Imaging System with Automatic Disparity Warping and Seaming", Graphical Models and Image Processing, Vol. 60, No. 3, May, 1998, pp. 196-208.

Figure 11 presents a block diagram of an electronic imaging  
10 system in accordance with a further embodiment of the present invention. The electronic imaging system **1100**, which is the system described in Figure 10, generates the composite digital image **1012**. The composite digital image is then projected onto a planar surface by techniques well known in the art to form a projected composite digital image **1102**.

15 The invention has been described with reference to a preferred embodiment. However, it will be appreciated that variations and modifications can be effected by a person of ordinary skill in the art without departing from the scope of the invention.

## PARTS LIST

|      |                           |
|------|---------------------------|
| 100  | camera                    |
| 102  | lens                      |
| 104  | imaging sensor            |
| 200  | optical image             |
| 202  | surface                   |
| 204  | imaging element           |
| 206  | output line               |
| 300  | chip body                 |
| 302  | circular array            |
| 304  | elements                  |
| 306  | elements                  |
| 308  | elements                  |
| 310  | axis                      |
| 400  | rectangular array         |
| 402  | image                     |
| 500  | image data                |
| 502  | addresses                 |
| 600  | imaging sensor            |
| 602  | array of imaging elements |
| 700  | imaging sensor            |
| 702  | array of imaging elements |
| 800  | imaging sensor            |
| 802  | cylindrical surface       |
| 804  | nodal point               |
| 806  | cylindrical axis          |
| 900  | imaging sensor            |
| 902  | spherical surface         |
| 904  | nodal point               |
| 1000 | lens                      |
| 1002 | optical image             |

- 1004 image sensor
- 1006 output signal
- 1007 digital camera
- 1008 source digital images
- 1010 image combining step
- 1012 composite digital image
- 1100 electronic imaging system
- 1102 projected composite digital image

and the first step is to determine the location of the object in the image. This is done by finding the center of mass of the object. The center of mass is the point where the object would balance if it were suspended from that point. This is done by finding the average of the x and y coordinates of all the pixels in the object. Once the center of mass is found, the location of the object is determined. The next step is to determine the size of the object. This is done by finding the area of the object. The area is the number of pixels in the object. The size of the object is then determined by dividing the area by the area of a single pixel. The final step is to determine the shape of the object. This is done by finding the perimeter of the object. The perimeter is the number of pixels on the boundary of the object. The shape of the object is then determined by dividing the perimeter by the perimeter of a single pixel.